



Mutations Mutations are involutions.	Minimal mutation-infinite quivers Image: Comparison of the second se
Mutation at vertex k takes an adjacency matrix $B = (b_{i,j})$ to $B' = (b'_{i,j})$ where $b'_{i,j} = \begin{cases} -b_{i,j} & \text{if } i = k \text{ or } j = k \\ b_{i,j} + \frac{ b_{i,k} b_{k,j}+b_{i,k} b_{k,j} }{2} & \text{otherwise} \end{cases}$	Minimal mutation-infinite quivers Universe and mutations Universe and mutations
Mutation-equivalent if there is a sequence of mutations	Minimal mutation-infinite quivers Quivers and mutations Mutation-equivalent Quivers P and Q are mutation-equivalent if there is a sequence of mutations $\mu_{i_1}, \ldots, \mu_{i_n}$ such that $P = \mu_{i_1} \circ \cdots \circ \mu_{i_n}(Q)$ This is an equivalence relation, and the equivalence classes under this relation are called mutation-classes .



Mutations do not preserve minimal mutation-infinite property	Minimal mutation-infinite quivers Image: Comparison of the problem of the proble
Why are minimal mutation-infinite quivers interesting? Any quiver containing a minimal mutation-infinite subquiver is necessarily mutation-infinite. A complete classification would give a systematic approach to check whether any given quiver is mutation-infinite or not.	Minimal mutation-infinite quivers Lever control Quivers and mutations Lever control Lever MMI quivers provide an computation free way of checking whether a given quiver is mutation-finite or mutation-infinite. Check whether any minimal mutation-infinite quiver can be embedded as a subquiver in the initial quiver. If it can, then the quiver is mutation-infinite. Check whether is mutation-infinite. If the quiver is mutation-infinite. If the quiver is mutation-infinite. If the quiver is mutation-infinite.
Ahmet Seven's classification of minimal infinite-type diagrams Seven classified all the infinite-type diagrams such that removing a vertex yielded a finite-type diagram.	Minimal mutation-infinite quivers Quivers and mutations Ahmet Seven's classification This is very similar to the work I am attempting on the minimal mutation-infinite quivers.

Felikson, Shapiro and Tumarkin started studying minimal mutation-infinite quivers In their paper on classifying mutation-finite quivers, FST proved that there were no minimal mutation-infinite quivers with more than 10 vertices.	Winimal mutation-infinite quivers
Minimal mutation-infinite quivers	Minimal mutation-infinite quivers Menod mutation definite quivers U-Quivers and mutations Menod mutation definite quivers U-Minimal mutation-infinite quivers Menod mutation definite quivers
Distinguished family of minimal mutation-infinite quivers which are orientations of simply-laced Coxeter diagrams of hyperbolic Coxeter simplices.	It is a result of Felikson, Shapiro and Tumarkin that the maximum number of vertices in a minimal mutation-infinite quiver is 10. This coincides with the sizes of hyperbolic Coxeter diagrams, as they exist up to size 10. This motivated the study of MMI quivers coming from these hyperbolic Coxeter diagrams.
Coxeter simplex convex hull of <i>n</i> + 1 points	Minimal mutation-infinite quivers Coxeter simplices, groups and diagrams Coxeter simplex
Considered inside spherical, Euclidean or hyperbolic space. $n + 1$ hyper-planes H_i with dihedral angles $\frac{\pi}{k_{ij}}$ (or possibly 0) between H_i and H_j . $\frac{\pi}{3}$ $\frac{\pi}{3}$ $\frac{\pi}{3}$ $\frac{\pi}{3}$	The faces of the simplex can be extended to hyperplanes. As it is a simplex, all such hyperplanes will intersect any other, and will do so at a dihedral angle. The requirement that the angles are submultiples of π is precisely what makes them Coxeter simplices.



and many more	Winimal mutation-infinite quivers
Sink-source mutations preserve minimal mutation-infinite-ness A sink-source mutation does not affect the underlying unoriented graph of a quiver and does not change the mutation class of any subquivers.	Minimal mutation-infinite quivers -Coxeter simplices, groups and diagrams
Result	Result for quivers up to size 9
Any minimal mutation-infinite quiver can be transformed through sink source mutations and at most 10 moves to either * a hyperbolic Coxeter simplex diagram * a double arrow quiver * an exceptional quiver	Any minimal mutation-infinite quiver can be transformed through sink-source mutations and at most 5 moves to either * a hyperbolic Coxeter simplex diagram * a double arrow quiver * an exceptional quiver

Result

Any minimal mutation-infinite quiver can be transformed through sink source mutations and at most 10 moves to either

- * a hyperbolic Coxeter simplex diagram
- $\star\,$ a double arrow quiver
- * an exceptional quiver